

THEORETICAL PROBABILITY

Theoretical Probability → the ratio of the number of outcomes that make up an event to the total number of possible outcomes.

$$P(A) = \frac{n(A)}{n(S)}$$

A: set of outcomes deemed successful.

S: set of all possible outcomes (sample space).

$n(A)$ or $n(S)$: the number of elements in each set.

- $P(\bar{A})$: Probability of event A not occurring.
- $P(\bar{A}) = 1 - P(A)$: Probability of a complement event.
- If A is a set of outcomes in S , then \bar{A} is the set of outcomes in S , that are not in A .
- Notations for complement to set A : A^c, \bar{A}, A'
- Note: $n(A) + n(\bar{A}) = n(S)$

Ex1. A bag contains 5 blue, 3 red, and 2 yellow blocks. One block is randomly selected. Find:

a) $P(\text{blue}) =$

b) $P(\text{red}) =$

c) $P(\overline{\text{red}}) =$

Ex 2. In a deck of cards, one is randomly selected. Find:

a) $P(\text{facecard}) =$

b) $P(\overline{\text{facecard}}) =$

Ex 3. Two coins are tossed. Find the probability of:

a) both heads

b) one head and one tail

Ex 4. Four coins are tossed. Find the probability of: (use a Tree Diagram)

a) 3 heads and 1 tail

b) 4 tails

c) 2 heads and 2 tails

Ex 5. Two dice are tossed. Find the probability of each element.

- a) A: sum is 11
- b) B: dice outcome differ by 3
- c) C: exactly one die is a 5
- d) D: neither die is a 5
- e) E: $P(\overline{A})$

Sum		Die 1					
		1	2	3	4	5	6
Die 2	1						
	2						
	3						
	4						
	5						
	6						